# Hall effect in strongly correlated electron systems

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This work provides a brief survey of the Hall effect data collected for some strongly correlated electron systems. The experimental results illustrate the behaviour of the heavy-fermion system UCu<sub>5</sub>Al, heavy-fermion semiconductor  $U_2Ru_2Sn$ , ferromagnetic superconductor under pressure UGe<sub>2</sub>, and the ferromagnet with a weak 2D localization effect UCo<sub>0.5</sub>Sb<sub>2</sub>.

Key words: Hall effect; strongly correlated electron system; heavy fermion system

## 1. Introduction

Over the last three decades, strongly correlated electron systems (SCES) have attracted an increased attention of many experimental and theoretical solid-state scientists around the world. The essential property of f-electron SCES is the instability of the f-electron shell and, in consequence, f-electrons in compounds with sp- and delements easily hybridise with conduction electrons. It is well known that the Hall resistivity of magnetic materials consists of normal  $R_0$  (OHE) and anomalous  $R_s$ (AHE) contributions. While the normal Hall effect results from the Lorenz force, the AHE is related to an asymmetric probability of electron scattering on magnetic centres. This means that the Hall effect could be a good probe for both electronic and magnetic properties in SCES. Recently, we have reported the Hall effect measurements on some U-based SCES, such as the heavy-fermion (HF) antiferromagnet UCu<sub>5</sub>AI [1], HF semiconductor U<sub>2</sub>Ru<sub>2</sub>Sn [2], ferromagnetic superconductor under pressure UGe<sub>2</sub> [3], and low-carrier density ferromagnet with a weak 2-dimensional localisation effect UCo<sub>0.5</sub>Sb<sub>2</sub> [4]. In this contribution, some outstanding and interesting features of these investigations will be outlined and highlighted.

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### 2. Results

The temperature dependences of the Hall coefficient  $R_H$  for the studied compounds are shown in Fig. 1. At high temperatures  $R_H$  is proportional to the magnetic susceptibility (*M/B*). For UCu<sub>5</sub>Al and U<sub>2</sub>Ru<sub>2</sub>Sn, the Hall effect data can be described based on skew scattering theory [5]. The  $R_H$  data for UGe<sub>2</sub> and UCo<sub>0.5</sub>Sb<sub>2</sub> can also be decomposed into negative  $R_0$  and positive  $R_s$  components. In all the samples, the extraordinary contribution (Table 1) was found to be dominant, indicating that the  $R_H(T)$ dependence is mainly due to incoherent skew scattering by U 5f moments. Carrier concentration at room temperature, estimated in a one-band model from  $R_0$  values, ranges from 0.4 for UGe<sub>2</sub>, 0.8 for UCo<sub>0.5</sub>Sb<sub>2</sub>, 1.2 for U<sub>2</sub>Ru<sub>2</sub>Sn to 4.9 e/f.u. for UCu<sub>5</sub>Al.



Fig. 1. Temperature dependence of the Hall coefficients of UCu<sub>5</sub>Al,  $U_2Ru_2Sn$ , UGe<sub>2</sub>, and UCo<sub>0.5</sub>Sb<sub>2</sub>. The solid lines represent fits (see text)

Compound	$R_s [m^3/C]$	γ <sub>1</sub> [K/T]	$R_0 [\mathrm{m}^3/\mathrm{C}]$	<i>n</i> [f.u.]	<i>m</i> <sup>*</sup> [m.e.]
UCu <sub>5</sub> Al, $H \parallel c$		0.08	$-6.44 \times 10^{-10}$	0.9	105
$U_2Ru_2Sn$		0.38	$-5 \times 10^{-10}$	0.04	48
$UGe_2, H \parallel c$	$3.7 \times 10^{-6}$		$-9.4 \times 10^{-10}$	3.1	15
$UCo_{0.5}Sb_2, H \parallel c$	$1.3 \times 10^{-5}$		$-1.96 \times 10^{-10}$	0.02	70

Table 1. Hall parameters derived from the fit of the experimental data

\*Fit to the equations  $R_H = R_0 + R_{s,\mu b}M/B$  and  $R_H = R_0 + \gamma_1 \rho M/B$ , where  $\gamma_1$  is a parameter related to the phase shift, *M* is magnetisation, *B* – magnetic induction, *n* – is charge carrier concentration at 2 K, and *m* \* – the effective mass at 2 K.

A different behaviour of the investigated compounds is observed at low temperatures. A remarkable feature is the increase in  $R_H$  for UCu<sub>5</sub>Al below 50 K. At 2 K,  $R_H$  achieves the value of  $9 \times 10^{-9}$  m<sup>3</sup>/C, corresponding to 0.9 carriers per f.u. Taking  $\gamma = 210$  mJ/(K<sup>2</sup>·mol U) [1], one can estimate the electron effective mass  $m^* = 105 m_e$ . This enhancement of the electron mass points out that a development of the heavyfermion state occurs in this compound at low temperatures.



Fig. 2. Temperature dependence of the charge carrier concentration n of UGe<sub>2</sub>, measured with a field applied perpendicular to the 010 and 001 directions

For U<sub>2</sub>Ru<sub>2</sub>Sn, the  $R_H$  (*T*) dependence shows a broad positive maximum at about 80 K and changes its sign below 50 K. At 2 K,  $R_H$  reaches the value of  $-1.5 \times 10^{-8}$  m<sup>3</sup>/C, which corresponds to a single-band concentration of n = 0.04 e/f.u. In the temperature range 15–80 K, the n(T) dependence can be described with the help of an exponential law with the energy gap of about 60 K. The latter value is comparable with those derived from the specific heat and NMR studies at 70 and 80 K, respectively [2]. All these features point to a gap opening in U<sub>2</sub>Ru<sub>2</sub>Sn.

Physical properties of UGe<sub>2</sub> are very unusual. Under the pressure of ~12 kbar, superconductivity with  $T_{SC} = 0.8$  K coexists with ferromagnetism [6]. It has also been pointed out that there exists a close relation between  $T_{SC}$  and  $T^*$ . The latter temperature is a characteristic temperature, visible in the temperature dependence of resistivity and tending to  $T_{SC}$  on increasing pressure. In the ordered state, the coefficients  $R_0$  and  $R_s$  of UGe<sub>2</sub> have been separated using  $R_H(B)$  and M(B) data simultaneously. Interestingly, the  $R_0$  coefficient displays a distinct anomaly at  $T^*$ . In consequence, the charge carrier concentration calculated within the single-band model has an upturn with decreasing temperature below  $T^*$  (Fig. 2). This phenomenon can be understood in terms of the so-called "dual nature" of 5f-electrons. Assuming that a hybridisation between the 5f and conduction electrons takes place below  $T^*$ , one can explain not only the carrier concentration, but also the enhancement of the density of states, and the itinerant behaviour of 5f electrons at low temperatures.

The Hall coefficient of UCo<sub>0.5</sub>Sb<sub>2</sub> increases rapidly with decreasing temperature below 100 K. This behaviour is associated with a decrease in the carrier concentration. At 2 K, *n* falls to 0.024 e/f.u (Fig. 3), making UCo<sub>0.5</sub>Sb<sub>2</sub> a low carrier system. It should be emphasised that the Hall mobility in UCo<sub>0.5</sub>Sb<sub>2</sub> changes sharply with temperature. It passes through a maximum of 450 cm<sup>2</sup>/(V·s) at 20 K and decreases by as

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Fig. 3. Temperature dependence of the charge carrier concentration of  $UCo_{0.5}Sb_2$ . The inset shows mobility as a function of temperature

many as two orders of magnitude, i.e. to  $3.7 \text{ cm}^2/(\text{V}\cdot\text{s})$  at T = 2 K (see the inset in Fig. 3). This change is probably related to a decrease in the carrier collision time. The Hall mean free path  $\lambda$ , estimated from  $R_H(T)$  and resistivity, also shows a dramatic drop, falling from about 350 Å at 20 K to 12 Å at 2 K. The temperature dependences of  $\mu$  and  $\lambda$  may support the weak localization effect suggested previously [4].

## 3. Summary

This work is an attempt to show some important results obtained by the measurements of the Hall coefficient on four 5f electron-based compounds (UCu<sub>5</sub>Al,  $U_2Ru_2Sn$ , UGe<sub>2</sub>, UCo<sub>0.5</sub>Sb<sub>2</sub>). Though these materials have different ground states, they belong to the so-called SCES family. The Hall effect data provided evidence of the enhancement of electron effective masses in all the studied compounds and shed new light on the behaviour associated with electron correlations.

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